# Package: greeks (via r-universe)

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**Title** Sensitivities of Prices of Financial Options and Implied Volatilities

Version 1.4.3

**Description** Methods to calculate sensitivities of financial option prices for European, geometric and arithmetic Asian, and American options, with various payoff functions in the Black Scholes model, and in more general jump diffusion models. A shiny app to interactively plot the results is included. Furthermore, methods to compute implied volatilities are provided for a wide range of option types and custom payoff functions. Classical formulas are implemented for European options in the Black Scholes Model, as is presented in Hull, J. C. (2017), Options, Futures, and Other Derivatives. In the case of Asian options, Malliavin Monte Carlo Greeks are implemented, see Hudde, A. & Rüschendorf, L. (2023). European and Asian Greeks for exponential Lévy processes. <doi:10.1007/s11009-023-10014-5>. For American options, the Binomial Tree Method is implemented, as is presented in Hull, J. C. (2017).

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# **Contents**

	Binomial_American_Greeks	2
	BS_European_Greeks	4
	BS_Geometric_Asian_Greeks	5
	BS_Implied_Volatility	6
	BS_Malliavin_Asian_Greeks	7
	Greeks	8
	Greeks_UI	11
	Implied_Volatility	12
	Malliavin_Asian_Greeks	14
	Malliavin_European_Greeks	15
	Malliavin_Geometric_Asian_Greeks	17
Index		19

Binomial\_American\_Greeks

Computes the Greeks of an American call- or put-option with the Binomial options pricing model

# **Description**

In contract to European Options, American options can be executed at any time until the expiration date. For more details on the definition of Greeks in general see Greeks. This functions computes Greeks of American put- and call options in the binomial option pricing model (see (Hull, 2022)).

## Usage

```
Binomial_American_Greeks(
  initial_price = 100,
  exercise_price = 100,
  r = 0,
  time_to_maturity = 1,
  volatility = 0.3,
  dividend_yield = 0,
  payoff = "call",
  greek = c("fair_value", "delta", "vega", "theta", "rho", "epsilon", "gamma"),
```

```
steps = 1000,
eps = 1/1e+05
```

# Arguments

initial\_price • initial price of the underlying asset. exercise\_price • strike price of the option. • risk-free interest rate. time\_to\_maturity • time to maturity. volatility • volatility of the underlying asset. dividend\_yield • dividend yield. payoff • the payoff function, a string in ("call", "put"). greek • the Greek to be calculated. • the number of integration steps. steps • the step size for the finite difference method to calculate theta, vega, rho eps and epsilon

## Value

Named vector containing the values of the Greeks specified in the parameter greek.

## References

Hull, J. C. (2022). Options, futures, and other derivatives (11th Edition). Pearson

## See Also

Greeks\_UI for an interactive visualization

## **Examples**

```
Binomial_American_Greeks(initial_price = 100, exercise_price = 100,
r = 0, time_to_maturity = 1, volatility = 0.3, dividend_yield = 0,
payoff = "call", greek = c("fair_value", "delta", "vega", "theta", "rho",
"epsilon", "gamma"), steps = 20)
```

BS\_European\_Greeks Computes the Greeks of a European call- or put-option, or of digital options in the Black Scholes model.

## **Description**

For details on the definition of Greeks see Greeks.

## Usage

## **Arguments**

```
• initial price of the underlying asset
initial_price
exercise_price
                     • strike price of the option
                     • risk-free interest rate
time_to_maturity
                     • time to maturity in years
volatility
                     · volatility of the underlying asset
dividend_yield
                     · dividend yield
payoff
                     • in c("call", "put", "cash_or_nothing_call", "cash_or_nothing_put", "asset_or_nothing_call",
                       "asset_or_nothing_put")
                     • Greeks to be calculated in c("fair_value", "delta", "vega", "theta", "rho",
greek
                       "epsilon", "lambda", "gamma", "vanna", "charm", "vomma", "veta", "vera",
                       "speed", "zomma", "color", "ultima")
```

## Value

Named vector containing the values of the Greeks specified in the parameter greek.

# See Also

```
Malliavin_European_Greeks for the Monte Carlo implementation
Greeks_UI for an interactive visualization
```

## **Examples**

```
BS_European_Greeks(initial_price = 120, exercise_price = 100, r = 0.02, time_to_maturity = 4.5, dividend_yield = 0.015, volatility = 0.22, greek = c("fair_value", "delta", "gamma"), payoff = "put")
```

BS\_Geometric\_Asian\_Greeks

Computes the Greeks of a Geometric Asian Option with classical Calland Put-Payoff in the Black Scholes model

# **Description**

For the definition of geometric Asian options see Malliavin\_Geometric\_Asian\_Greeks. BS\_Geometric\_Asian\_Greeks offers a fast and exaction computation of Geometric Asian Greeks.

# Usage

```
BS_Geometric_Asian_Greeks(
  initial_price = 100,
  exercise_price = 100,
  r = 0,
  time_to_maturity = 1,
  volatility = 0.3,
  dividend_yield = 0,
  payoff = "call",
  greek = c("fair_value", "delta", "rho", "vega", "theta", "gamma")
)
```

#### **Arguments**

```
initial_price
                     • initial price of the underlying asset, can also be a vector
exercise_price
                      · strike price of the option
                      • risk-free interest rate
time_to_maturity
                      · time to maturity in years
volatility

    volatility of the underlying asset

dividend_yield

    dividend yield

payoff
                     • the payoff function, either a string in ("call", "put")
greek
                     • the Greeks to be calculated in c("fair_value", "delta", "vega", "theta", "rho",
                        "gamma", "vomma")
```

#### Value

Named vector containing the values of the Greeks specified in the parameter greek.

## See Also

Malliavin\_Geometric\_Asian\_Greeks for the Monte Carlo implementation which provides digital and custom payoff functions and also works for the jump diffusion model

Greeks\_UI for an interactive visualization

## **Examples**

```
BS_Geometric_Asian_Greeks(initial_price = 110, exercise_price = 100, r = 0.02, time_to_maturity = 4.5, dividend_yield = 0.015, volatility = 0.22, greek = c("fair_value", "delta", "rho", "vega", "theta", "gamma"), payoff = "put")
```

BS\_Implied\_Volatility Computes the implied volatility for European put- and call options in the Black Scholes model via Halley's method.

# **Description**

For the definition of *implied volatility* see Implied\_Volatility. BS\_Implied\_Volatility offers a very fast implementation for European put- and call options applying Halley's method (see en.wikipedia.org/wiki/Halley%27s\_method).

## Usage

```
BS_Implied_Volatility(
  option_price,
  initial_price = 100,
  exercise_price = 100,
  r = 0,
  time_to_maturity = 1,
  dividend_yield = 0,
  payoff = "call",
  start_volatility = 0.3,
  precision = 1e-09
)
```

```
    option_price
    current price of the option
    initial_price
    initial price of the underlying asset.
    exercise_price
    strike price of the option.
    r isk-free interest rate.
    time_to_maturity
    time to maturity.
```

```
    dividend_yield
    dividend yield.
    the payoff function, a string in ("call", "put").
    start_volatility
    the volatility value to start the approximation
    precision
    precision of the result
```

#### Value

Named vector containing the values of the Greeks specified in the parameter greek.

## See Also

Implied\_Volatility for American and Asian options, and for digital payoff functions

# **Examples**

```
BS_Implied_Volatility(option_price = 27, initial_price = 100, exercise_price = 100, r = 0.03, time_to_maturity = 5, dividend_yield = 0.015, payoff = "call")
```

```
BS_Malliavin_Asian_Greeks
```

Computes the Greeks of an Asian option with the Malliavin Monte Carlo Method in the Black Scholes model

# Description

For a description of Asian Greeks see Malliavin\_Asian\_Greeks. BS\_Malliavin\_Asian\_Greeks offers a fast implementation in the Black Scholes model.

#### **Usage**

```
BS_Malliavin_Asian_Greeks(
  initial_price = 100,
  exercise_price = 100,
  r = 0,
  time_to_maturity = 1,
  volatility = 0.3,
  dividend_yield = 0,
  payoff = "call",
  greek = c("fair_value", "delta", "vega", "rho"),
  steps = round(time_to_maturity * 252),
  paths = 1000,
  seed = 1
)
```

8 Greeks

## Arguments

initial\_price • initial price of the underlying asset, can also be a vector exercise\_price • strike price of the option, can also be a vector • risk-free interest rate time\_to\_maturity · time to maturity in years · volatility of the underlying asset volatility dividend\_yield · dividend yield payoff • the payoff function, either a string in ("call", "put"), or a function • Greeks to be calculated in c("fair\_value", "delta", "rho", "vega") greek • the number of integration steps steps paths • the number of simulated paths seed • the seed of the random number generator

#### Value

Named vector containing the values of the Greeks specified in the parameter greek.

#### See Also

Malliavin\_Asian\_Greeks for a greater set of Greeks and also in the jump diffusion model Greeks\_UI for an interactive visualization

# **Examples**

```
BS_Malliavin_Asian_Greeks(initial_price = 110, exercise_price = 100, r = 0.02, time_to_maturity = 4.5, dividend_yield = 0.015, volatility = 0.22, greek = c("fair_value", "delta", "rho"), payoff = "put")
```

Greeks

Computes the Greeks of various options in the Black Scholes model or both in the Black Scholes model or a Jump Diffusion model in the case of Asian Options, or in the Binomial options pricing model

## **Description**

Greeks are derivatives of the option value with respect to underlying parameters. For instance, the Greek  $\Delta = \frac{\partial fair\_value}{\partial initial\_price}$  (Delta) measures how the price of an option changes with a minor change in the underlying asset's price, while  $\Gamma = \frac{\partial fair\_value}{\partial initial\_price}$  (Gamma) measures how  $\Delta$  itself changes as the price of the underlying asset shifts. Greeks can be computed for different types of options: For

- European Greeks see also BS\_European\_Greeks and Malliavin\_European\_Greeks
- American Greeks see also Binomial\_American\_Greeks

Greeks 9

- Asian Greeks see also BS\_Malliavin\_Asian\_Greeks and Malliavin\_Asian\_Greeks
- Geometric Asian Greeks see also BS\_Geometric\_Asian\_Greeks and Malliavin\_Asian\_Greeks

The Greeks are defined as the following partial derivatives of the option value:

- Delta =  $\Delta = \frac{\partial fair\_value}{\partial initial\_price}$ , the derivative with respect to the price of the underlying asset
- Vega =  $\mathcal{V} = \frac{\partial fair\_value}{\partial volatility}$ , the derivative with respect to the volatility
- Theta =  $\Theta = -\frac{\partial \text{fair\_value}}{\partial \text{time\_to\_maturity}}$ , the negative derivative with respect to the time until expiration of the option
- rho =  $\rho = \frac{\partial \text{fair\_value}}{\partial r}$ , the derivative with respect to the risk-free interest rate
- Epsilon =  $\epsilon = \frac{\partial fair\_value}{\partial time\_to\_maturity}$ , the derivative with respect to the dividend yield of the underlying asset
- Lambda =  $\lambda = \Delta \times \frac{\text{initial\_price}}{\text{exercise\_price}}$
- Gamma =  $\Gamma = \frac{\partial^2 fair\_value}{\partial initial\_price^2}$ , the second derivative with respect to the price of the underlying asset
- Vanna =  $\frac{\partial \Delta}{\partial \text{volatility}} = \frac{\partial^2 \text{fair\_value}}{\partial \text{intial\_price} \, \partial \text{volatility}}$ , the derivative of  $\Delta$  with respect to the volatility
- Vomma =  $\frac{\partial^2 fair\_value}{\partial volatility^2}$ , the second derivative with respect to the volatility
- Veta =  $\frac{\partial \mathcal{V}}{\partial r} = \frac{\partial^2 \text{fair\_value}}{\partial \text{volatility } \partial \text{time\_to\_maturity}}$ , the derivative of  $\mathcal{V}$  with respect to the time until expiration of the option
- Vera =  $\frac{\partial^2 \text{fair\_value}}{\partial \text{volatiliv } \partial r}$ , the derivative of  $\mathcal{V}$  with respect to the risk-free interest rate
- Speed =  $\frac{\partial \Gamma}{\partial \text{initial\_price}} = \frac{\partial^3 \text{fair\_value}}{\partial \text{initial\_price}^3}$ , the third derivative of the option value with respect to the price of the underlying asset
- Zomma =  $\frac{\Gamma}{\text{volatility}} = \frac{\partial^3 fair\_value}{\partial \text{volatility}^3}$ , the derivative of Gamma with respect to the volatility
- Color =  $\frac{\partial \Gamma}{\partial r} = \frac{\partial^3 fair\_value}{\partial initial\_price^2 \partial r}$ , the derivative of Gamma with respect to the risk-free interest rate
- Ultima =  $\frac{\partial Vomma}{\partial volatility} = \frac{\partial^3 fair\_value}{\partial volatility^3}$ , the third derivative with respect to the volatility

Greeks computes Greeks for the following option types:

- European put- and call options, which give to option holder the right but not the obligation to sell (resp. buy) the underlying asset for a specific price at a specific date. If K is the exercise price, and  $S_T$  the value of the underlying asset at time-to-maturity T, a European options pay off the following amount at expiration:
  - $\max\{K S_T, 0\}$  for a put-option
  - $\max\{S_T K, 0\}$  for a call-option
- American put- and call options are like European options, but allow the holder to exercise
  at any time until expiration
- European cash-or-nothing put- and call options provide the holder with a fixed amount of cash, if the value of the underlying asset is below (resp. above) a certain strike price
- European asset-or-nothing put- and call options are similar to cash-or-nothing options, but provide the holder with one share of the asset.

10 Greeks

• Asian put- and call options have a similar payoff to European put- and call options but differ from European options in that they are path dependent. Not the price  $S_T$  of the underlying asset at time-to-maturity T is evaluated, but the arithmetic average  $\frac{1}{T} \int_0^T S_t dt$ . We get the payoffs

```
- \max\{K - \frac{1}{T} \int_0^T S_t dt, 0\} for an Asian put-option
- \max\{\frac{1}{T} \int_0^T S_t dt - K, 0\} for an Asian call-option
```

• Geometric Asian options differ from Asian options in that the geometric average  $\exp\left(\frac{1}{T}\int_0^T \ln S_t dt\right)$  is evaluated.

For reference see Hull (2022) or en.wikipedia.org/wiki/Greeks\_(finance).

# Usage

```
Greeks(
  initial_price,
  exercise_price,
  r,
  time_to_maturity,
  volatility,
  dividend_yield = 0,
  model = "Black_Scholes",
  option_type = "European",
  payoff = "call",
  greek = c("fair_value", "delta", "vega", "theta", "rho", "gamma"),
  antithetic = TRUE,
  ...
)
```

```
• initial price of the underlying asset
initial_price
exercise_price
                     • strike price of the option
                     • risk-free interest rate
time_to_maturity
                     • time to maturity in years
volatility
                     · volatility of the underlying asset
dividend_yield
                     · dividend yield
                     • the model to be chosen in ("black_scholes", "jump_diffusion")
model
                  in c("European", "American", "Asian", "Geometric Asian", "Digital", "Bino-
option_type
                  mial) - the type of option to be considered
                     • in c("call", "put", "cash_or_nothing_call", "cash_or_nothing_put", "asset_or_nothing_call",
payoff
                       "asset_or_nothing_put")
                     • Greeks to be calculated in c("fair_value", "delta", "vega", "theta", "rho",
greek
                       "epsilon", "lambda", "gamma", "vanna", "charm", "vomma", "veta", "vera",
                       "speed", "zomma", "color", "ultima")
```

Greeks\_UI

```
antithetic
```

- if TRUE, antithetic random numbers will be chosen to decrease variance
- ... Other arguments passed on to methods

#### Value

Named vector containing the values of the Greeks specified in the parameter greek.

#### References

```
Hull, J. C. (2022). Options, futures, and other derivatives (11th Edition). Pearson en.wikipedia.org/wiki/Greeks_(finance)
```

#### See Also

```
BS_European_Greeks for option_type = "European"

Binomial_American_Greeks for option_type = "American"

BS_Geometric_Asian_Greeks for option_type == "Geometric Asian" and model = "black_scholes"

BS_Malliavin_Asian_Greeks for option_type == "Asian" and model = "black_scholes" and greek in c("fair_value", "delta", "rho", "vega")

Malliavin_Asian_Greeks for more general cases of Asian Greeks

Greeks_UI for an interactive visualization
```

## **Examples**

```
Greeks(initial_price = 100, exercise_price = 120, r = 0.01,
time_to_maturity = 5, volatility = 0.30, payoff = "call")

Greeks(initial_price = 100, exercise_price = 100, r = -0.005,
time_to_maturity = 1, volatility = 0.30, payoff = "put",
option_type = "American")
```

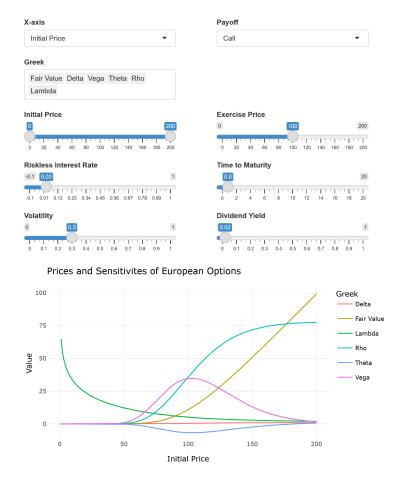
Greeks\_UI

Opens a shiny app to interactively visualize option prices and Greeks.

## **Description**

Opens a shiny app to interactively visualize option prices and Greeks. This works for European Options (see BS\_European\_Greeks), American Options (see Binomial\_American\_Greeks), Geometric Asian Options (see BS\_Geometric\_Asian\_Greeks), as well as Asian options (see BS\_Malliavin\_Asian\_Greeks). For performance reasons, just the Black-Scholes model is possible, and for some cases, the set of Greeks is limited. On the y-Axis, the option value resp. the value of the greeks are displayed, for the x-axis, several parameters like initial\_price or time\_to\_maturity are possible.

12 Implied\_Volatility



# Usage

Greeks\_UI()

Implied\_Volatility Computes the implied volatility for various options via Newton's method

# Description

If the value of an option, and other (model)parameters like the risk-free interest rate, the time-to-maturity, and the dividend yield are known, the assumed volatility of the underlying asset, the *implied volatility* can be inferred. See Hull (2022).

## Usage

```
Implied_Volatility(
  option_price,
```

Implied\_Volatility 13

```
initial_price = 100,
  exercise_price = 100,
  r = 0,
  time_to_maturity = 1,
  dividend_yield = 0,
  model = "Black_Scholes",
  option_type = "European",
  payoff = "call",
  start_volatility = 0.3,
  precision = 1e-06,
  max_iter = 30
)
```

# **Arguments**

```
• current price of the option
option_price
initial_price
                    • initial price of the underlying asset
                    • strike price of the option
exercise_price
                    • risk-free interest rate
time_to_maturity
                    • time to maturity in years
dividend_yield
                    · dividend yield
model
                    • the model to be chosen
                  in c("European", "American", "Geometric Asian", "Asian", "Digital") - the type
option_type
                  of option to be considered
payoff
                    • in c("call", "put")
start_volatility
                  initial guess
                  precision of the computation
precision
max_iter
                  maximal number of iterations of the approximation
```

#### Value

Named vector containing the values of the Greeks specified in the parameter greek.

## References

```
Hull, J. C. (2022). Options, futures, and other derivatives (11th Edition). Pearson
```

## See Also

```
BS_Implied_Volatility for the special case option_type = "European" and payoff in c("call", "put")
```

# Examples

```
Implied_Volatility(15, r = 0.05, option_type = "Asian",
payoff = "call")
```

Malliavin\_Asian\_Greeks

Computes the Greeks of an Asian option with the Malliavin Monte Carlo Method in the Black Scholes model, or for Asian options, also in a Jump Diffusion model

# **Description**

Asian options are path-dependent. If  $S_t$  is the price of the underlying asset at time t, the execution of an Asian option depends on the average price of option,  $\frac{1}{T}\int_0^T S_t dt$ , where T is the time-to-maturity of the option. For more details on the definition of Greeks in general see Greeks.

For a description of Malliavin Monte Carlo Methods for Greeks see for example (Hudde & Rüschendorf, 2023).

# Usage

```
Malliavin_Asian_Greeks(
  initial_price = 100,
  exercise_price = 100,
  r = 0.
  time_to_maturity = 1,
  volatility = 0.3,
  dividend_yield = 0,
  payoff = "call",
  greek = c("fair_value", "delta", "rho", "vega", "theta", "gamma"),
  model = "black_scholes",
  lambda = 0.2,
  alpha = 0.3,
  jump_distribution = function(n) stats::rt(n, df = 3),
  steps = round(time_to_maturity * 252),
  paths = 10000,
  seed = 1,
  antithetic = FALSE
)
```

```
    initial_price
    initial price of the underlying asset, can also be a vector
    strike price of the option, can also be a vector
    r isk-free interest rate
    time_to_maturity
    time to maturity in years
    volatility
    volatility of the underlying asset
    dividend_yield
    dividend yield
```

payoff	• the payoff function, either a string in ("call", "put", "digital_call", "digital_put"), or a function	
greek	• the Greek to be calculated	
model	• the model to be chosen in ("black_scholes", "jump_diffusion")	
lambda	• the lambda of the Poisson process in the jump-diffusion model	
alpha	• the alpha in the jump-diffusion model influences the jump size	
jump_distribution		
	• the distribution of the jumps, choose a function which generates random numbers with the desired distribution	
steps	• the number of integration steps	
paths	• the number of simulated paths	
seed	• the seed of the random number generator	
antithetic	• if TRUE, antithetic random numbers will be chosen to decrease variance	

#### Value

Named vector containing the values of the Greeks specified in the parameter greek.

#### References

Hudde, A., & Rüschendorf, L. (2023). European and Asian Greeks for Exponential Lévy Processes. Methodol Comput Appl Probab, 25 (39). doi:10.1007/s11009023100145

## See Also

BS\_Malliavin\_Asian\_Greeks for a faster computation, but only in the Black Scholes model and with a smaller set of Greeks

# **Examples**

```
Malliavin_Asian_Greeks(initial_price = 110, exercise_price = 100,
r = 0.02, time_to_maturity = 4.5, dividend_yield = 0.015, volatility = 0.22,
greek = c("fair_value", "delta", "rho"), payoff = "put")
```

Malliavin\_European\_Greeks

Computes the Greeks of a European option with the Malliavin Monte Carlo Method in the Black Scholes model

# **Description**

For details on the definition of Greeks see Greeks. For a description of Malliavin Monte Carlo Methods for Greeks see for example (Hudde & Rüschendorf, 2023).

## Usage

```
Malliavin_European_Greeks(
  initial_price = 100,
  exercise_price = 100,
  r = 0,
  time_to_maturity = 1,
  volatility = 0.3,
  payoff = "call",
  greek = c("fair_value", "delta", "vega", "theta", "rho", "gamma"),
  model = "Black Scholes",
  paths = 10000,
  seed = 1,
  antithetic = FALSE
)
```

## **Arguments**

• initial price of the underlying asset initial\_price • strike price of the option exercise\_price • risk-free interest rate time\_to\_maturity • time to maturity in years volatility · volatility of the underlying asset payoff • the payoff function, either a string in ("call", "put", "cash\_or\_nothing\_call", "cash\_or\_nothing\_call", "asset\_or\_nothing\_call", "asset\_or\_nothing\_put"), or a function • the Greeks to be calculated in ("fair\_value", "delta", "vega", "theta", "rho", greek "gamma") • the model to be chosen model • the number of simulated paths paths • the seed of the random number generator seed antithetic • if TRUE, antithetic random numbers will be chosen to decrease variance

# Value

Named vector containing the values of the Greeks specified in the parameter greek

#### References

Hudde, A., & Rüschendorf, L. (2023). European and Asian Greeks for Exponential Lévy Processes. Methodol Comput Appl Probab, 25 (39). doi:10.1007/s11009023100145

## See Also

BS\_European\_Greeks for the exact and fast implementation for call-, put- and digital payoff functions

## **Examples**

```
Malliavin_European_Greeks(initial_price = 110,
exercise_price = 100, r = 0.02, time_to_maturity = 4.5,
volatility = 0.22, greek = c("fair_value", "delta", "rho"), payoff = "put")
```

Malliavin\_Geometric\_Asian\_Greeks

Computes the Greeks of a geometric Asian option with the Malliavin Monte Carlo Method in the Black Scholes- or Jump diffusion model

# **Description**

In contrast to Asian options (see Malliavin\_Asian\_Greeks), geometric Asian options evaluate the geometric average  $\exp\left(\frac{1}{T}\int_0^T \ln S_t dt\right)$ , where  $S_t$  is the price of the underlying asset at time t and T is the time-to-maturity of the option (see

en.wikipedia.org/wiki/Asian\_option#European\_Asian\_call\_and\_put\_options\_with\_geometric\_averaging). For more details on the definition of Greeks see Greeks, and for a description of the Malliavin Monte Carlo Method for Greeks see for example (Hudde & Rüschendorf, 2023).

## Usage

```
Malliavin_Geometric_Asian_Greeks(
  initial_price = 100,
  exercise_price = 100,
  r = 0,
  time_to_maturity = 1,
  volatility = 0.3,
  dividend_yield = 0,
  payoff = "call",
  greek = c("fair_value", "delta", "rho", "vega", "theta", "gamma"),
  model = "black_scholes",
  lambda = 0.2,
  alpha = 0.3,
  jump_distribution = function(n) stats::rt(n, df = 3),
  steps = round(time_to_maturity * 252),
  paths = 10000,
  seed = 1,
  antithetic = FALSE
)
```

```
    initial_price
    initial price of the underlying asset, can also be a vector
    exercise_price
    strike price of the option, can also be a vector
    r isk-free interest rate
```

time\_to\_maturity • time to maturity in years volatility · volatility of the underlying asset · dividend yield dividend\_yield • the payoff function, either a string in ("call", "put", "digital\_call", "digipayoff tal\_put"), or a function greek · the Greek to be calculated mode1 • the model to be chosen in ("black\_scholes", "jump\_diffusion") lambda • the lambda of the Poisson process in the jump-diffusion model alpha • the alpha in the jump-diffusion model influences the jump size jump\_distribution • the distribution of the jumps, choose a function which generates random numbers with the desired distribution • the number of integration steps steps paths • the number of simulated paths seed • the seed of the random number generator antithetic • if TRUE, antithetic random numbers will be chosen to decrease variance

#### Value

Named vector containing the values of the Greeks specified in the parameter greek.

#### References

Hudde, A., & Rüschendorf, L. (2023). European and Asian Greeks for Exponential Lévy Processes. Methodol Comput Appl Probab, 25 (39). doi:10.1007/s11009023100145

## See Also

BS\_Geometric\_Asian\_Greeks for exact and fast computation in the Black Scholes model and for put- and call payoff functions

## **Examples**

```
Malliavin_Asian_Greeks(initial_price = 110, exercise_price = 100, r = 0.02, time_to_maturity = 4.5, dividend_yield = 0.015, volatility = 0.22, greek = c("fair_value", "delta", "rho"), payoff = "put")
```

# **Index**

```
Binomial_American_Greeks, 2, 8, 11
BS_European_Greeks, 4, 8, 11, 16
BS_Geometric_Asian_Greeks, 5, 5, 9, 11, 18
BS_Implied_Volatility, 6, 6, 13
BS_Malliavin_Asian_Greeks, 7, 9, 11, 15
Greeks, 2, 4, 8, 9, 14, 15, 17
Greeks_UI, 3, 4, 6, 8, 11, 11
Implied_Volatility, 6, 7, 12
Malliavin_Asian_Greeks, 7-9, 11, 14, 17
Malliavin_European_Greeks, 4, 8, 15
Malliavin_Geometric_Asian_Greeks, 5, 6, 17
```